

P.K.R. ARTS COLLEGE FOR WOMEN (AUTONOMOUS)

(Accredited with 'A' grade by NAAC - Affiliated to Bharathiar University, Coimbatore)

GOBICHETTIPALAYAM – 638 476

DEPARTMENT OF MATHEMATICS

MASTER OF SCIENCE IN MATHEMATICS



Syllabus

For the candidates admitted from the Academic Year 2020-2021 and onwards

Under CBCS PATTERN

MASTER OF MATHEMATICS

Course Scheme and Scheme of Examinations

(For students admitted from 2020-2021 and onwards)

| Part | Category | Course Code | Title of the Course | ContactHrs/ week | Exam Duration hrs. | Max.Marks | | | Credits |
|----------------------|-------------|-------------|---|------------------|--------------------|-----------|-----|-------|---------|
| | | | | | | CIA | ESE | Total | |
| SEMESTER - I | | | | | | | | | |
| III | Core: I | 20MAP01 | Advanced Algebra | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core :II | 20MAP02 | Real Analysis | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core : III | 20MAP03 | Ordinary Differential Equations | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core : IV | 20MAP04 | Measure Theory and Integration | 5 | 3 | 25 | 75 | 100 | 4 |
| III | Elective I | 20MAP05A | Numerical Analysis | 5 | 3 | 25 | 75 | 100 | 4 |
| | | 20MAP05B | Control Theory | | | | | | |
| III | Core : V | 20MAP06 | Programming in Python - Practical | 2 | 3 | 40 | 60 | 100 | 2 |
| III | Core : VI | 20MAP07 | Comprehension in Mathematics - I (Self Study Course - Online Exam) | - | 1½ | - | 100 | 100 | 1 |
| | | | TOTAL | 30 | | | | 700 | 23 |
| SEMESTER - II | | | | | | | | | |
| III | Core :VII | 20MAP08 | Complex Analysis | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core : VIII | 20MAP09 | Partial Differential Equations | 5 | 3 | 25 | 75 | 100 | 4 |
| III | Core : IX | 20MAP10 | Classical Mechanics | 5 | 3 | 25 | 75 | 100 | 4 |
| III | Core :X | 20MAP11 | Differential Geometry | 5 | 3 | 25 | 75 | 100 | 4 |

| | | | | | | | | | |
|-----|--------------------------|----------------------|---|----|----|-----|-----|-----|----|
| III | Elective II | 20MAP12A 20MAP12B | Mathematical Statistics Programming in C++ | 5 | 3 | 25 | 75 | 100 | 4 |
| III | Elective-II Practical | 20MAP13A 20MAP13B | Mathematical Software - I (SPSS) - Practical Programming in C++ - Practical | 2 | 3 | 40 | 60 | 100 | 2 |
| III | Ability Enhancement | 20AEPMA01 | Cyber Security | 2 | 3 | 100 | - | 100 | 2 |
| III | Core : XI | 20MAP14 | Comprehension in Mathematics - II (Self Study Course - Online Exam) | - | 1½ | - | 100 | 100 | 1 |
| | | | TOTAL | 30 | | | | 800 | 25 |

SEMESTER - III

| | | | | | | | | | |
|-----|----------------------------|----------------------|--|----|----|----|-----|-----|----|
| III | Core : XII | 20MAP15 | Topology | 6 | 3 | 25 | 75 | 100 | 5 |
| III | Core : XII | 20MAP16 | Theory of Numbers | 6 | 3 | 25 | 75 | 100 | 5 |
| III | Core : XIV | 20MAP17 | Optimization Techniques | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core : XV | 20MAP18 | Mathematical Software - II (R Software) - Practical | 3 | 3 | 40 | 60 | 100 | 2 |
| IV | Open Elective | *** | OPTIONAL | 3 | 3 | 25 | 75 | 100 | 3 |
| V | Proficiency Enhancement | 20PEPMA01 | Industrial Mathematics (Self Study) | - | 3 | - | 100 | 100 | 2 |
| III | Elective III | 20MAP19A 20MAP19B | Graph Theory Integral Transforms | 6 | 3 | 25 | 75 | 100 | 4 |
| III | Core : XVI | 20MAP20 | Comprehension in Mathematics - III (Self Study Course - Online Exam) | - | 1½ | - | 100 | 100 | 1 |
| | | | TOTAL | 30 | | | | 800 | 26 |

SEMESTER - IV

| | | | | | | | | | | |
|-----|-------------|----------|---|-----------------|---|----|-----|-----|----|-----|
| III | Core :XVII | 20MAP21 | Functional Analysis | 6 | 3 | 25 | 75 | 100 | 3 | |
| III | Core: XVIII | 20MAP22 | Mathematical Methods | 6 | 3 | 25 | 75 | 100 | 4 | |
| III | Core :XIX | 20MAP23 | Fluid Dynamics | 6 | 3 | 25 | 75 | 100 | 4 | |
| III | Core :XX | 20MAP24 | Project Work & Viva Voce | 6 | 3 | 20 | 80 | 100 | 4 | |
| III | Elective IV | 20MAP25A | Fuzzy Logic and Fuzzy Sets | 6 | 3 | 25 | 75 | 100 | 4 | |
| | | 20MAP25B | Actuarial Mathematics | | | | | | | |
| III | Core :XXI | 20MAP26 | Comprehension in Mathematics - IV (Self Study Course - Online Exam) | | | | 100 | 100 | 1 | |
| | | | Total | 30 | | | | 600 | 22 | |
| | | | Online Course / Learning Object Repository | I - IV SEMESTER | | | | | | 2 |
| | | | Certificate Course | I - IV SEMESTER | | | | | | 2 |
| | | | Total Marks - 2000 Credits - | | | | | | | 100 |

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Gobichettipalayam-638476

DEPARTMENT OF MATHEMATICS

M.Sc.DEGREE PROGRAMME

SEMESTER I

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------|--------------------|----------------------------|-----------|----------|---------------|
| CORE | 20MAP01 | ADVANCED ALGEBRA | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about algebraic structures, theory of groups, rings and fields.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|--|---|
| CO1 | gain deep knowledge about various algebraic structures. | K₁ |
| CO2 | understand the concepts from simple groups to extension field. | K₂ |
| CO3 | apply the algebraic methods for solving problems. | K₃& K₅ |

| | | |
|------------|--|-------------------------------------|
| CO4 | recognize some advanced results of the theory of groups, rings and fields. | K₄ |
| CO5 | solve the problems by using various algebraic structures. | K₅, K₆ |

UNIT I: GROUP THEORY (15 Hours)

Another counting principle – Sylow’s theorem – Direct products.

UNIT II: RING THEORY (15 Hours)

Euclidean rings – A particular Euclidean ring – Polynomial rings – Polynomials over the rational field.

UNIT III: FIELDS (15 Hours)

Extension Fields – Roots of polynomials – More about roots.

UNIT IV: FIELDS (Continuation) (15 Hours)

Elements of Galois theory – Finite Fields.

UNIT V: LINEAR TRANSFORMATIONS (12 Hours)

Canonical forms: Triangular form – Trace and Transpose – Hermitian, unitary and normal Transformations.

TEXT BOOK:

Herstein.I.N (Reprint 2017)– “Topics in Algebra”, 2nd Edition, Wiley Indian Pvt.Ltd,New Delhi-110002.

| UNIT | CHAPTER | SECTION |
|------------|------------------------|---------------------------|
| I | II | 2.11 to 2.13 |
| II | III | 3.7 to 3.10 |
| III | V | 5.1,5.3 and 5.5 |
| IV | V VII | 5.6 7.1. |
| V | VI | 6.4, 6.8 and 6.10 |

REFERENCE BOOKS:

1. Fraleigh.J.B.(2003) – “A First Course in Abstract Algebra”,3rd Edition Narosa Publishing House, New Delhi.
2. Artin.M (1991)– “Algebra”, Prentice-Hall, Englewood Cliff.
3. Hungerford.T.W.(1974) – “Algebra”, Springer, New York.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------|----|---|--------|
| CORE | 20MAP02 | REAL ANALYSIS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about Riemann Stiltjes Integral, Sequence and Series of functions and Functions of Several Variables.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | understand the axiomatic foundation of the real number system | K ₁ |
| CO2 | define and recognize the series of real numbers and convergence and define the basic terms under Riemann Stiltjes Integral and Uniform Convergence | K ₁ & K ₂ |
| CO3 | analyze the concepts of convergence criteria and linear transformation. | K ₄ |
| CO4 | apply the concept of Uniform convergence to find the convergence criteria of a certain function. | K ₃ |
| CO5 | evaluate the Riemann Stiltjes integral and Derivatives of Higher Order | K ₅ , K ₆ |

UNIT I: THE RIEMANN STILTJES INTEGRAL (15 Hours)

Definition and Existence of the Integral –Properties of the integral –Integration and Differentiation –Integration of vector valued function .

UNIT II: SEQUENCE AND SERIES OF FUNCTIONS (15 Hours)

Uniform convergence - Uniform convergence and continuity –Uniform convergence and integration .

UNIT III:SEQUENCE AND SERIES OF FUNCTIONS (Continued....)(15 Hours)

Uniform convergence and differentiation –Equicontinuous families of functions – The Stone Weirstrass theorem.

UNIT IV: FUNCTIONS OF SEVERAL VARIABLES (15 Hours)

Linear transformation –Contraction principle.

UNIT V:FUNCTIONS OF SEVERAL VARIABLES (Continued....) (12 Hours)

Inverse function theorem –Implicit function theorem – Determinants – Differentiation of Integrals.

TEXT BOOKS:

1. Rudin.W–(2017) “Principles of Mathematical Analysis”, Third edition, McGraw Hill Education Pvt.ltd, New York.

| UNIT | CHAPTER | PAGE NUMBER |
|------|---------|------------------|
| I | 6 | 120-134 |
| II | 7 | 143-152 |
| III | 9 | 152-165 |
| IV | 3 | 204-211, 220-221 |
| V | 4 | 221-228, 231-238 |

REFERENCE BOOKS:

- 1.RobertG.Bartle and Donald R.Sherbert (2010), Third Edition, ”Introduction to Real Analysis”, John Wiley and sons.
2. RudinW(2012), “Real and complex Analysis”, McGraw- Hill, New York, 3rd Edition,

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------------------|----|---|--------|
| CORE | 20MAP03 | ORDINARY DIFFERENTIAL EQUATIONS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about linear differential equations, systems of linear and Non-linear differential equations and their solutions.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | define ordinary point, Legendre equation, Bessel equation, Fundamental matrix, Picard's theorem and oscillations of solutions. | K ₁ |
| CO2 | understand the existence and uniqueness of solutions of systems of linear differential equations and Non-linear initial value problems. | K ₂ |
| CO3 | Identify and analyze the results in systems of linear differential equations and Non-linear initial value problems. | K ₃ & K ₄ |
| CO4 | construct the solutions of systems of linear differential equations and Non-linear initial value problems and analyze the oscillations of solutions of second order differential equations. | K ₄ , K ₆ |

| | | |
|------------|--|--|
| CO5 | apply power series method and successive approximation method to evaluate the solutions of systems of linear differential equations and Non-linear initial value problems. | K₃&K₅ |
|------------|--|--|

UNIT I: SOLUTIONS IN POWER SERIES

(15 Hours)

Second order linear equations with ordinary points – Legendre equation and Legendre polynomials – Second order equations with regular singular points – Bessel function

UNIT II: SYSTEMS OF LINEAR DIFFERENTIAL EQUATIONS

(15 Hours)

Systems of first order equations – Existence and uniqueness theorem – Fundamental matrix.

UNIT III: SYSTEMS OF LINEAR DIFFERENTIAL EQUATIONS(continuation) (15 Hours)

Non-homogeneous linear systems – Linear systems with constant coefficients – Linear systems with periodic co-efficients.

UNIT IV: EXISTENCE AND UNIQUENESS OF SOLUTIONS

(15 Hours)

Successive approximations – Picard’s theorem - Non-uniqueness of solution – Continuation and dependence on initial conditions, Existence of solutions in the large – Existence and uniqueness of solutions of systems.

UNIT V: OSCILLATIONS OF SECOND ORDER EQUATIONS

(12 Hours)

Fundamental results – Sturm’s comparison theorem – Elementary linear oscillations. Comparison theorem of Hille-Wintner – Oscillations of $x'' + a(t)x = 0$.

TEXT BOOK:

S.G.Deo, V.Lakshmikanthan and V.Raghavendra “Ordinary Differential Equations”, Second Edition- Seventh reprint 2004, Tata McGraw-Hill Publishing company Limited, New Delhi.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|------------------|
| I | III | 3.2 – 3.5 |
| II | IV | 4.2 – 4.5 |
| III | IV | 4.6 – 4.8 |
| IV | V | 5.1 – 5.8 |
| V | VIII | 8.1 – 8.5 |

REFERENCE BOOKS:

1. Coddington.E.A. andLevinson.N., (1955), “Theory of Ordinary Differential Equations”, McGraw Hill, New York.
2. George F.Simmons(1974),” Differential Equations with applications And Historical Notes”, Tata McGraw Hill, New York.
3. V.Dharmaiah“ Introduction to theory of OrdineryDifferenitil Equations”, PHI Learning Private Limited.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|--------------------------------|----|---|--------|
| CORE | 20MAP04 | MEASURE THEORY AND INTEGRATION | 60 | - | 4 |

Preamble :

To enable the students to learn and gain knowledge about the concepts of measurable sets and measurable spaces.

Course Outcomes

On the successful completion of the course, students will be able to

| CO Number | CO Statement | Knowledge Level |
|-----------|--|---------------------------------|
| CO1 | Understand the concept of Lebesgue measure in measurable sets | K ₂ |
| CO2 | Define the concept of Lebesgue integral of a bounded measurable function and measurable nonnegative function | K ₁ |
| CO3 | Apply differentiation and integration in monotone functions | K ₃ |
| CO4 | Analyze integration of measurable functions over general measure spaces | K ₄ |
| CO5 | Evaluate the construction of product Measures and Lebesgue measure on Euclidean space | K ₅ , K ₆ |

UNIT I :Lebesgue Measure**(12 Hours)**

Introduction – Lebesgue Outer Measure – The σ – Algebra of Lebesgue Measurable Sets – Outer and Inner Approximation of Lebesgue Measurable Sets – Countable Additivity, Continuity and the Borel–Cantelli Lemma.

UNIT II :Lebesgue Integration**(12 Hours)**

The Riemann Integral – The Lebesgue Integral of a Bounded Measurable Function over a Set of Finite Measure – The Lebesgue Integral of a Measurable Nonnegative Function –The General Lebesgue Integral.

UNIT III : Differentiation and Integration**(12 Hours)**

Continuity of Monotone Functions – Differentiability of Monotone Functions: Lebesgue’s Theorem – Functions of Bounded Variations: Jordan’s Theorem.

UNIT IV :Integration over General Measure Spaces**(12 Hours)**

Measurable Functions – Integration of Nonnegative Measurable Functions– The Radon–Nikodym Theorem.

UNIT V :The Construction of Particular Measures**(12 Hours)**

Product Measures: The Theorems of Fubini and Tonelli.

TEXT BOOK :

H.L. Royden, P.M. Fitzpatrick (2014) - “Real Analysis”, 4th Edition, PHI Learning Private Limited, Delhi.

| UNITS | CHAPTER | SECTIONS | PAGE No |
|--------------|----------------|------------------------|-------------------------|
| I | 2 | 2.1–2.5 | 29-47 |
| II | 4 | 4.1–4.4 | 68-89 |
| III | 6 | 6.1–6.3 | 107-118 |
| IV | 18 | 18.1–18.2, 18.4 | 359-371, 381-385 |
| V | 20 | 20.1 | 414-422 |

REFERENCE BOOKS :

1. Bartle R.G (1976) - "Elements of Real Analysis", 2nd Edition, John Wiley and Sons, New York.
2. Rudin W(1986) - "Real and complex Analysis", 3rd Edition, McGraw– Hill, New York.
3. Tom M.Apostol(2002)- "Mathematical Analysis", 2nd Edition , Narosa Publishing House, New Delhi.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|------------|-------------|---------------------|----|---|--------|
| ELECTIVE I | 20MAP05A | NUMERICAL ANALYSIS | 60 | - | 4 |

Preamble :

To enable the students to learn and gain knowledge about numerical differentiation, integration, Solution of system of both ordinary and partial differential equations.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|--|
| CO1 | understand the concept of numerical differentiation, integration, solution of system of both ordinary and partial differential equations. | K₁ & K₂ |
| CO2 | analyze the various methods in characteristic value problems. | K₄ |
| CO3 | remember the formulae for central difference formulae, numerical differentiation, integration and also write the formulae for various methods. | K₁ |
| CO4 | apply Euler's method, Taylor series method to solve the problems numerically. | K₃, K₆ |

| | | |
|------------|---|--|
| CO5 | learn how to solve the problems numerically by using direct, indirect methods, single step and multistep methods and also the problems based on non linear equations. | K₂ & K₅ |
|------------|---|--|

UNIT I: CENTRAL DIFFERENCE INTERPOLATION FORMULAE (15 Hours)

Central Difference table – Gauss’s forward interpolation formula - Gauss’s Backward interpolation formula – Stirling’s formula.

UNIT II: NUMERICAL DIFFERENTIATION (12 Hours)

Introduction – Newton’s forward difference formula to compute the derivatives - Newton’s backward difference formula to compute the derivatives – Problems – Derivatives using Stirling’s formula – Maxima and minima of a tabulated function.

Numerical Integration: Numerical Integration – The Trapezoidal Rule – Simpson’s 1/3rd and Simpson’s 3/8th Rules.

UNIT III: SOLUTION OF ORDINARY DIFFERENTIAL EQUATIONS (15 Hours)

Taylor series method –Euler and Modified Euler methods –Rungekutta methods (Fourth Order)–Multistep methods –Milne’s method –Adams Moulton method.

UNIT IV: NUMERICAL SOLUTION OF PARTIAL DIFFERENTIAL EQUATIONS (15 Hours)

(Solutions of Elliptic, Parabolic and Hyperbolic partial differential equations)
 Elliptic Equation –Laplace’s equation on a rectangular region –Iterative methods for Laplace equation –Parabolic Equation-Hyperbolic Equation .

UNIT V: CHARACTERISTIC VALUE PROBLEMS (15 Hours)

Characteristic value problems –Eigen values of a matrix by Iteration –The power method- Jacobi Methods for finding Eigen values & Eigen vectors .

TEXT BOOK:

1. Sastry S.S (2005) -“Introductory Methods of Numerical Analysis ”, Prentice-Hall of India Private limited, New Delhi-110001.

2.Dr.P.Kandasamy,Dr.K.Thilagavathi,Dr.K.Gunavathi(2005)-“Numerical Methods”, S.Chand & Company LTD, New Delhi-110055.

| UNIT | BOOK | CHAPTER | SECTION |
|------|------|---------|----------------------------------|
| I | I | III | 3.7.1-3.7.2 |
| II | I | V | 5.1-5.4.3 (omit 5.2.1, 5.2.2) |
| III | I | VII | 7.2, 7.4, 7.4.2, 7.5- 7.6 |
| IV | II | XII | 12.5-12.10 |
| V | II | XIII | 13 |

REFERENCE BOOKS:

1. Chapra.S.C. and Raymond.P.C. (2000) – “ Numerical Methods for Engineers”, Tata McGraw Hill, New Delhi.

2. Burden.R.L. and Douglas Faires.J. (1989) – “ Numerical Analysis”, Fourth Edition, P.W.S.Kent Publishing Company, Boston .

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|---------------------|--------------------|----------------------------|-----------|----------|---------------|
| ELECTIVE - I | 20MAP05B | CONTROL THEORY | 60 | - | 4 |

Preamble

To enable the students to gain the knowledge about modeling the control systems using difference equations.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|--|--|
| CO1 | understand the mathematical tools that are needed to solve differential equations. | K₂ |
| CO2 | gain the knowledge about research methodology. | K₁ |
| CO3 | identify the differential equation models to the real system. | K₄ |
| CO4 | learn how to use the various techniques of control systems. | K₂ & K₃ |
| CO5 | evaluate the different types of equations to solve real life problems. | K₅, K₆ |

Unit I: OBSERVABILITY: (12 Hours)

Linear Systems –ObservabilityGrammian –Constant coefficient systems –Reconstruction kernel – Nonlinear Systems.

Unit II: CONTROLLABILITY: (12 Hours)

Linear systems –Controllability Grammian – Adjoint systems –Constant coefficient systems –steering function –Nonlinear systems.

Unit III:STABILITY: (12 Hours)

Stability –Uniform Stability –Asymptotic Stability of Linear Systems.

Unit IV:STABILITY (Continuation) (12 Hours)

Perturbed linear systems –Nonlinear systems – OPTIMAL CONTROL: Linear time varying systems.

Unit V:STABILIZABILITY: (12 Hours)

Stabilization via linear feedback control –Bass method –Controllable subspace –Stabilization with restricted feedback.

TEXT BOOK :

Balachandran.K and Dauer.J.P.(2012)– “Elements of Control Theory”, 2nd edition, Narosa, New Delhi.

| UNIT | CHAPTER | PAGE NO. |
|------|---------|-------------------------------|
| I | 2 | 21 - 38 |
| II | 3 | 40 – 56 |
| III | 4 | 75 - 81 |
| IV | 4, 6 | 82 – 91, 119 – 128, 130 -131, |
| V | 5 | 100 - 117 |

REFERENCE BOOKS:

1. Conti .R (1976) – “Linear Differential Equations and Control”, Academic Press, London.
2. Curtain.R.F. andPritchard.A.J.(1977) – “ Functional Analysis and Modern Applied Mathematics”, Academic Press, New York.
3. Klamka.J (1991) – “Controllability of Dynamical Systems”, Kluwer Academic Publisher, Dordrecht.
4. Russell.D.L. (1979) – “Mathematics of Finite Dimensional Control Systems” , Marcel Dekker, New York.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------|------------------------|--|----------|-----------|---------------|
| CORE | 20MAP06 | PROGRAMMING IN PYTHON - PRACTICAL | - | 24 | 2 |

LIST OF PROGRAMS

All the following listed programs have to be executed and recorded

1. Write a program to create a class and object in Python.
2. Write a program to find correlation coefficient between the variables.
3. Write a program to find the probability of a prime number appearing when a 20 sided die is rolled.
4. Write a program to find standard deviation for the given set of values.
5. Write a program to calculate the mean, median and mode using Python.
6. Write a program to convert temperature from Celcius to Fahrenheit and vice versa.
7. Write a program for finding the roots of quadratic function.
8. Write a program to solve the initial value problem using Runge - Kutta method.
9. Write a program to solve ordinary differential equation using Python.
10. Write a Python program to calculate distance between two points using latitude and longitude.

SEMESTER II

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------|----|---|--------|
| CORE | 20MAP08 | COMPLEX ANALYSIS | 72 | - | 4 |

Preamble :

To enable the students to learn the concept of complex number system.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | understand the fundamental concepts of complex number system and analytic functions | K ₁ |
| CO2 | define analytic function, Residues , Taylor series , Laurent series and mappings. | K ₁ & K ₂ |
| CO3 | apply Cauchy's theorem , Taylor's Theorem , Residue theorem , Weierstrass's Theorem, Riemann Mapping theorem for the analytic function. | K ₃ |
| CO4 | analyzesingularities,complex integration and power series expansion. | K ₄ |
| CO5 | evaluate integrals along a path in the complex plane, branch points. | K ₅ , K ₆ |

UNIT I: INTRODUCTION TO THE CONCEPT OF ANALYTIC FUNCTION

(19 Hours)

Limits and continuity – Analytic functions – Polynomials – Rational functions.

Conformality: Arcs and closed curves – Analytic functions in regions – Conformal Mapping – Length and Area – Linear Transformations: The Linear group – The Cross ratio – Elementary Riemann Surfaces.

UNIT II: COMPLEX INTEGRATION

(19 Hours)

Line Integrals - Rectifiable Arcs – Line Integrals as Functions of Arcs – Cauchy's theorem for a rectangle - Cauchy's theorem in a disk- Cauchy's Integral formula: The Index of a point with respect to a closed curve – The Integral formula – Higher derivatives - Removable singularities, Taylor's Theorem – Zeros and Poles – The Local Mapping– The Maximum principle – Chains and cycles.

UNIT III: THE CALCULUS OF RESIDUES

(12 Hours)

The Residue theorem – The Argument principle – Harmonic functions: Definitions and basic Properties – The Mean value property – Poisson's Formula.

UNIT IV: SERIES AND PRODUCT DEVELOPMENTS

(12 Hours)

Weierstrass's Theorem – The Taylor Series – The Laurent Series – Partial fractions and Factorization: Partial Fractions – Infinite Products – Canonical Products.

UNIT V: MAPPING THEOREM

(10 Hours)

The Riemann Mapping Theorem: Statement and Proof – Boundary Behaviour – Use of the reflection principle – Analytic Arcs – Conformal mapping of Polygons: The Behaviour at an angle – The Schwarz – Christoffel Formula – Mapping on a rectangle.

TEXT BOOK:

Ahlfors L.V. – (2014), "Complex Analysis" ,4thReprint , McGraw Hill Education (India) Pvt.LtdNew York.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|--|
| I | 2 | 1.1 – 1.4 |
| | 3 | 2.1 – 2.4, 3.1, 3.2 and 4.3 |
| II | 4 | 1.1 – 1.5, 2.1 – 2.3, 3.1 - 3.4,4.1 |
| III | 4 | 5.1 – 5.2, 6.1 – 6.3 |
| IV | 5 | 1.1 – 1.3, 2.1 – 2.3 |
| V | 6 | 1.1 – 1.4, 2.1 – 2.3 |

REFERENCE BOOK:

RuelV.Churchill(1990) – “Complex Variables and Applications”, Fifth Edition,McGraw – Hill International Editions.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|--------------------------------|----|---|--------|
| CORE | 20MAP09 | PARTIAL DIFFERENTIAL EQUATIONS | 60 | - | 4 |

Preamble :

To enable the students to learn and gain knowledge about Initial boundary- value problems, Methods for solving Partial Differential Equation and Green's function.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | gain the knowledge about hyperbolic, parabolic, elliptic type partial differential equations, method of separation of variables, initial and boundary value problems, Green's function. | K ₁ |
| CO2 | understand the classification of second order partial differential equations, D'Alembert's solution, existence and uniqueness of solutions, method of images. | K ₂ |
| CO3 | apply the method of separation of variables and method of Green's function to solve initial - boundary value problems. | K ₃ |
| CO4 | classify second order partial differential equations and analyze the solutions of initial and BVP. | K ₄ |
| CO5 | construct the solutions of second order partial differential equations and discuss the method of eigen functions. | K ₅ , K ₆ |

UNIT I: MATHEMATICAL MODEL**(12 Hours)**

The Classical equation – The vibrating string – The vibrating membrane – Conduction of heat in solids. Classification of second order equations: Second order equations in two independent variables – Canonical forms – Equations with constant coefficients – General solution.

UNIT II: THE CAUCHY PROBLEM**(12 Hours)**

The Cauchy problem – Cauchy – Kowalewskaya theorem – Homogeneous wave equation – Initial – Boundary value problems – Non-homogeneous boundary conditions – Non-homogeneous wave equation.

UNIT III: METHOD OF SEPARATION OF VARIABLES**(12 Hours)** Separation

of variables – The vibrating string problem – Existence and Uniqueness of solution of the vibrating string problem. The heat conduction problem – Existence and uniqueness of solution of the heat conduction problem – The Laplace and beam equations.

UNIT IV: BOUNDARY VALUE PROBLEMS**(12Hours)**

Boundary value problems – Maximum and minimum principles – Uniqueness and continuity theorems – Dirichlet problems for a circle – Dirichlet problems for a circular annulus – Neumann problem for a circle Dirichlet problem for a rectangle – Neumann problem for a rectangle.

UNIT V: GREEN'S FUNCTIONS**(12 Hours)**

The Dirac delta function – Properties of Green's function – Method of Green's functions – Dirichlet problem for the Laplace operator – Method of images – Method of Eigen functions.

TEXT BOOK:

TynMyint. U with LokenathDebnath (2007) – “Linear Partial Differential Equations for Scientists and Engineers”, 4th Edition ,Birkhusar Boston, New York.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|--------------------------------|
| I | III | 3.1 – 3.5 (omit 3.4) |
| | IV | 4.1 – 4.4 |
| II | V | 5.1 – 5.5,5.7 |
| III | VII | 7.1 – 7.6 |
| IV | IX | 9.1 – 9.9 (omit 9.8) |
| V | XI | 11.1 – 11.8 (omit 11.6) |

REFERENCE BOOKS

1. Evans.L.C., (2003) – “Partial Differential Equations”, AMS, Providence, R I.
2. Sneddon.I.N. (1957) - “Elements of Partial Differential Equations”, McGraw Hill, London.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------|----|---|--------|
| CORE | 20MAP10 | CLASSICAL MECHANICS | 60 | - | 4 |

Preamble :

To enable the students to learn and gain knowledge about mechanical systems.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|---------------------------------|
| CO1 | understand the notions of configuration space, generalised coordinates, canonical transformations and phase space in mechanics. | K ₁ & K ₂ |
| CO2 | analyze the Euler-Lagrange equations from a variational principle and Hamiltonian formulation of a mechanical system | K ₄ |
| CO3 | apply theoretical techniques including variational principles and Hamilton Jacobi Theory in mechanical systems. | K ₃ |
| CO4 | analyze theoretical techniques | K ₄ |
| CO5 | evaluate the cause of linear, rotational and rolling motions, by describing torques, work and energy, impulse and momentum associated with objects undergoing each type of motion. | K ₅ , K ₆ |

UNIT I: INTRODUCTORY CONCEPTS (12 Hours)

Mechanical system – Generalized coordinates – Constraints – Virtual work – Energy and momentum.

UNIT II: LAGRANGE’S EQUATIONS (12 Hours)

Derivations of Lagrange’s Equations– Examples-Integrals of motion.

UNIT III: HAMILTON’S EQUATIONS (12 Hours)

Hamilton’s Principle – Hamilton’s equations.

UNIT IV: HAMILTON – JACOBI THEORY (12 Hours)

Hamilton’s principle function – Hamilton – Jacobi equation.

UNIT V: CANONICAL TRANSFORMATIONS (12 Hours)

Differential forms and generating functions –Lagrange and Poisson brackets.

TEXT BOOK:

Greenwood.D.T. (1997) – “Classical Dynamics”, Dover Publication, New York.

| UNIT | CHAPTER | SECTION |
|------|---------|-----------|
| I | 1 | 1.1 - 1.5 |
| II | 2 | 2.1 – 2.3 |
| III | 4 | 4.1 – 4.2 |
| IV | 5 | 5.1 – 5.2 |
| V | 6 | 6.1,6.3 |

REFERENCE BOOKS:

1. Gupta.S.C,Kumar.V.Sharma.H.V.(2015)-“Classical Mechanics” K.K Mittal for PragattiPrakashan,Meerut.
2. Gupta.A.S.(2009)-“Calculus of Variation” PHI Learning pvt.ltd.Newdelhi.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|-----------------------|----|---|--------|
| CORE | 20MAP11 | DIFFERENTIAL GEOMETRY | 60 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about the space curves, fundamental forms and geodesic on a surface.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|---------------------------------|
| CO1 | gain the knowledge about the theory of space curves and surfaces | K ₁ |
| CO2 | understand the basic terms and tools of differential geometry | K ₂ |
| CO3 | determine the Gaussian curvature, principal curvatures and lines of curvatures of the curve | K ₃ |
| CO4 | analyse the nature of points on the space curve and surface and deduce the conditions that a point to be singular, ordinary, elliptic, etc.. | K ₄ |
| CO5 | Evaluate the fundamental quadratic forms, intrinsic and extrinsic forms of surface | K ₅ , K ₆ |

UNIT I : THEORY OF SPACE CURVES**(15 Hours)**

Introduction – Representation of space curves – Unique parametric representation of a space curve – Arc-length – Tangent and osculating plane – Principle normal and binormal – Curvature and torsion –Contact between curves and surfaces.

UNIT II : THEORY OF SPACE CURVES (CONTINUATION)**(15 Hours)**

Osculating circle and osculating sphere – Locus of centre of spherical curvature – Tangent surfaces – Involutives and Evolutes –Spherical indicatrix- Intrinsic equations of space curves – Fundamental existence theorem for space curves.

UNIT III : THE FIRST FUNDAMENTAL FORM**(10 Hours)**

The first fundamental form – Local intrinsic properties of a surface: Introduction - Definition of a surface – Nature of points on a surface – Representation of a surface – Curves on surfaces – Metric on a surface –The first fundamental form– Families of curves – Orthogonal trajectories – Double family of curves.

UNIT IV : THE SECOND FUNDAMENTAL FORM**(10 Hours)**

The Second Fundamental form and local non-intrinsic properties of a surface: Introduction – The Second fundamental form-Classification of points on a surface- Principal curvatures- Lines of curvature.

UNIT V : GEODESIC ON A SURFACE**(10 Hours)**

Normal property of Geodesics –Gaussian curvature-The Fundamental Equations of Surface Theory: Introduction – Tensor notations –Gauss equations –Weingarten equations-Mainardi-Codazzi equations.

TEXT BOOK:

Somasundaram.D (2010)– “Differential Geometry”, Fourth Reprint , Narosa Publishing House Pvt. Ltd., Chennai.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|----------------------------------|
| I | I | 1.1 - 1.7, 1.10 |
| II | I | 1.11 - 1.13 , 1.15 – 1.17 |
| III | II | 2.1 - 2.5, 2.9-2.13 |
| IV | IV | 4.1 - 4.5 |
| V | III | 3.5, 3.12, 5.1-5.5 |

REFERENCE BOOK

StruikD.T(1961)- “Lectures on Classical Differential Geometry”, Addison – Wesley, Publishing company INC.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-------------|-------------|-------------------------|----|---|--------|
| ELECTIVE II | 20MAP12A | MATHEMATICAL STATISTICS | 60 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about various probability distributions.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | define the concepts based on probability. | K ₁ |
| CO2 | analyze the various kinds of distribution functions. | K ₄ |
| CO3 | gain the knowledge about the different types of density functions. | K ₂ |
| CO4 | apply the concepts based on moment – generating functions to find the moments. | K ₃ |
| CO5 | evaluate the problems based on Uniform, Bernoulli, Binomial, Uniform, Exponential and Chi-Square Distributions. | K ₅ , K ₆ |

UNIT I : THEORY OF PROBABILITY**(12 Hours)**

Introduction – Sample spaces – Sample point – Discrete and Continuous sample spaces - Events – Venn diagrams – The probability of an Event – Rules of Probability.

UNIT II : PROBABILITY DISTRIBUTIONS**(12 Hours)**

Random variables – Discrete and Continuous Random Variables – Probability Distributions – Distribution function – Continuous Random Variables – Probability density functions.

UNIT III : MATHEMATICAL EXPECTATION**(12 Hours)**

Introduction – The expected value of a Random Variable – Moments - Chebyshev's theorem – Related Examples.

UNIT IV : SPECIAL PROBABILITY DISTRIBUTIONS**(12 Hours)**

Introduction – The Discrete Uniform Distribution – The Bernoulli Distribution – Bernoulli trial (Repeated trials) – The Binomial Distribution – Moment Generating function of Binomial Distribution – The Negative Binomial and Geometric Distributions.

UNIT V: SPECIAL PROBABILITY DENSITIES**(12 Hours)**

Introduction – The Uniform Distribution – Mean and Variance – The Gamma Distribution – Exponential Distribution – The Chi-Square Distribution.

TEXT BOOK :

Irwin Miller and Marylees Miller(2012) - "Mathematical Statistics ", Seventh Edition, Pearson Publications, New Delhi.

| UNIT | CHAPTER | SECTION |
|------|---------|-----------|
| I | II | 2.1 – 2.5 |
| II | III | 3.1 – 3.4 |
| III | IV | 4.1 – 4.4 |
| IV | V | 5.1 – 5.5 |
| V | VI | 6.1 – 6.3 |

REFERENCE BOOK :

Kapur.J.N and Saxena.H.C. (2011)- “Mathematical Statistics”, 20thEdition,
S.Chand&company, Ram Nagar, New Delhi.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|---------------|-------------|---------------------|----|---|--------|
| ELECTIVE - II | 20MAP12B | PROGRAMMING IN C++ | 60 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about C++ Programming such as Tokens, Expressions, Control Structure, Classes and Objects.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | Understand and apply the C++ structure, tokens, expressions, control structures | K ₁ & K ₂ |
| CO2 | Ability to declare various prototyping, friend and virtual functions | K ₃ |
| CO3 | Create Classes, objects, arrays of objects, constructors, and Destructors. | K ₃ & K ₄ |
| CO4 | Analyze over loading operators | K ₄ |
| CO5 | solve numerical problems by using C++ programs. | K ₅ & K ₆ |

UNIT - I : TOKENS, EXPRESSIONS AND CONTROL STRUCTURE (12 HOURS)

Basic Concept of Object Oriented Programming : Basic Concept of OOPS - Benefits of OOP – Application of OOP

Tokens, Expressions and Control Structure: Introduction – Tokens – Keywords – Identifiers and Constants – Basic Data Types – User Defined Data Types – Derived Data Types – Declaration of Variables – Dynamic Initialization of Variables – Reference Variables – Operators - Control Structures.

UNIT- II : FUNCTIONS IN C++**(12 HOURS)**

Functions in C++: Introduction – The Main Function – Function Prototyping – Call by Reference– Return by Reference – Inline Functions – Default Arguments – const Arguments – Recursion – Function Over Loading – Friend and Virtual Functions – Math Library Functions.

UNIT – III : CLASSES AND OBJECTS**(12 HOURS)**

Classes and Objects: Introduction – C Structures Revisited – Specifying a Class –Defining Member Functions – A C++ Program with Class – Making An Outside Function Inline –Nesting Of Member Functions – Private Member Functions – Arrays Within A Class –Arrays of Objects – Objects as Function Arguments – Friend Functions.

UNIT – IV : CONSTRUCTORS AND DESTRUCTORS**(12 HOURS)**

Constructors and Destructors: Introduction – Constructors – Parameterized Constructors – Multiple Constructors in a Class – Constructors with Default Arguments – Dynamic Initializations of Objects – Copy Constructor – Destructors.

UNIT – V : OPERATOR OVERLOADING**(12 HOURS)**

Operator Overloading: Introduction – Defining Operator Overloading – Overloading Unary Operators – Overloading Binary Operators – Overloading Binary Operators Using Friends – Manipulating of Strings Using Operators – Rules for Overloading Operators.

Text Book

E. Balaguruswamy, Object–Oriented Programming with C++, Seven Edition, Tata McGrawHill Publishing Company Limited.

| UNIT | CHAPTER | SECTION |
|------|---------|--|
| I | 1 & 3 | 1.5 – 1.8, 3.1 – 3.8, 3.11 - 3.14 and 3.25 |
| II | 4 | 4.1 – 4.12 |
| III | 5 | 5.1 – 5.15 |
| IV | 6 | 6.1 –6.11 |
| V | 7 | 7.1 – 7.8 |

Reference Books :

1 Programming with C++ by D. Ravichandran, -Tata McGraw Hill publishing company limited, New Delhi.

2 Object Oriented Programming with C++ by S.S.Vinod Chandra, New age publishing company limited.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------------------------------|------------------------|---|----------|-----------|---------------|
| ELECTIVE II PRACTICAL | 20MAP13A | MATHEMATICAL SOFTWARE – I (SPSS) - PRACTICAL | - | 24 | 2 |

LIST OF PROGRAMS

All the following listed programs have to be executed and recorded

1. Create a SPSS database and to find Mean.
2. Create a SPSS database and to find Median and Mode.
3. Find the Standard deviation, Variance and Range by using SPSS database.
4. Find the Standard error of Mean, Maximum and Minimum by using SPSS database.
5. Create a SPSS database and to find both Pearson's and Spearman's correlation in both 1- Tailed and 2-Tailed tests.
6. Create the SPSS database to fit the Straight line and plot the Exponential curve using Regression.
7. Create a SPSS database and present that data through charts and diagrams.
8. Find the probability distribution by using Binomial distribution in SPSS.
9. Find the probability distribution by using Poisson distribution in SPSS.
10. Find the probability distribution by using Normal distribution in SPSS.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------|-------------|---------------------|---|----|--------|
| PRACTICAL | 20MAP12B | PROGRAMMING IN C++ | - | 36 | 2 |

LIST OF PROGRAMS

All the following listed programs have to be executed and recorded

1. DISTANCE CONVERSION PROBLEM:

Create two classes DM and DB which store the value of distances. DM store the value of distances. DM stores distances in meters and centimeters in DB in feet and inches. Write a Program that can create the values of the class objects and add one object DM with another object DB. Use a friend function to carry out addition operation. The object that stores the result may be DM object or DB object depending on the units in which results are required. The display should be in the order of meter and centimeter and feet or inches depending on the order of display.

2. OVERLOADING OBJECTS:

Create a class FLOAT that contains one float data member overload all the four arithmetic operators so that operate on the objects of FLOAT.

3. OVERLOADING CONVERSIONS:

Design a class polar which describes a pant in a plane using polar Co-ordinates radius and angle. A point in polar Co-ordinates is as shown below. Use the overloader + operator to add two objects of polar. Note that we cannot add polar values of two points directly. This requires first the conversion. Points into rectangular Co-ordinates and finally converting the result into polar Co-ordinates. You need to use following trigonometric formulas. $X = r * \cos(a)$; $Y = r * \sin(a)$; $a = \tan^{-1}(\frac{Y}{X})$; $r = \text{sqrt}(X * X + Y * Y)$;

4. OVRELOADING MATRIX:

Create a class MAT of size M*N. Define all possible matrix operations for MAT type objects. Verify the identity. $(A-B)^2 = A^2 + B^2 - 2*A*B$

5. AREA COMPUTATION USING DERIVED CLASS:

Area of rectangle = $X*Y$

Area of triangle = $\frac{1}{2} * X * Y$

6. VECTOR PROBLEM:

Define a class for vector containing scalar values. Apply overloading concepts for vector addition, Multiplication of a vector by a scalar quantity, replace the values in a position vector.

7. INHERITANCE:

Create three classes alpha, beta and gamma, each containing one data member. The class gamma should be inherited from both alpha and beta. Use a constructor function in the class gamma to assign values to the data members of all the classes. Write a program to print the data members of all the three classes.

8. INLINE FUNCTION:

Create two inline functions that can return the multiplication and division for two data members.

9. STATIC DATA MEMBER:

Write a program to illustrate the use of static data member.

10. ARRAY OF OBJECT:

Create a class employee and illustrate the use of object array.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------------------------|--------------------|----------------------------|-----------|----------|---------------|
| ABILITY ENHANCEMENT | 20AEPMA01 | CYBER SECURITY | 24 | - | 2 |

Preamble

To understand the basics of cyber security and the security threats in day-to-day activities.

Course Outcomes

On the successful completion of the course, students will be able to

| CO Number | CO Statement | Knowledge Level |
|------------------|---|--|
| CO1 | understand the basic concepts of information security and its types | K₁ |
| CO2 | obtaining the knowledge thoroughly on cyber security and its principles | K₁ |
| CO3 | deals with risk management and threats | K₁&K₂ |
| CO4 | gain detailed knowledge on security issues in social media | K₃&K₄ |
| CO5 | apply and work with cyber security applications in real world | K₅&K₆ |

Unit I: INFORMATION SECURITY

(5 Hours)

History of Information Security - Need for Security-**Types of security:** Physical Security – Network security –Personal security –Operation security –Communication security - Information security threats.

Unit II: INTRODUCTION TO CYBER SECURITY (5 Hours)

Cyber Security: Objectives- Roles-Differences between Information Security and Cyber Security.**Cyber Security Principles:** Confidentiality- Integrity – Availability.

Unit III: RISKS & VULNERABILITIES (5 Hours)

Risk Meaning: Risk Management –Problems of Measuring Risk -Risk Levels-Risk Analyzes-Risk Assessment –Response to Risk Terminology- **Threats:** Components of Threats- Types of Threats- **Vulnerabilities:** Computing System Vulnerabilities –Hardware Vulnerabilities- Software Vulnerabilities-Data Vulnerabilities-Human Vulnerabilities.

Unit IV: SOCIAL MEDIA

(5 Hours)

Introduction to social media: What, Why –Pros and cons- **Security issues in social media:** Mail-Facebook-Whatsapp-Twitter-Preventive and control measures.

Unit V: CASE STUDY

(4 Hours)

Impact of social media: Education -Business- Banking-Mobile –Human Life- Present generation- Indian scenario.

WEB REFERENCES

1. <https://m.youtube.com/watch?v=o6pgd8gLFHg>
2. <https://m.youtube.com/watch?v=3r14ZjZpcHU>
3. <https://blog.barkly.com/10-fundamental-cybersecurity-lessons-for-beginners>
4. <https://5social media security risk and how to avoid them.html>
5. <https://10 cyber security twitter profiles to watch.html>
6. <https://cyber security in banking 4 trends to watch in 2017.html>
7. <https://gmail hacking security tips-indian cyber security solutions.html>
8. <https://why social media sites are the new cyber weapons of.html>
9. **EBook:A complete guide to Staying Ahead in the Cyber Security Game**

SEMESTER III

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------|----|---|--------|
| CORE | 20MAP15 | TOPOLOGY | 72 | - | 5 |

Preamble

To enable the students to learn and gain knowledge about Topological Space.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | understand the axioms of topological space, connected space, countability, separation, completely regular space, complete metric space. | K ₁ |
| CO2 | define and recognize the properties of general topological space, continuous function, metric space, compactness. | K ₁ &K ₂ |
| CO3 | apply the concepts of Urysohn lemma, Urysohn metrization theorem, the Tychonoff theorem and Ascoli's theorem in topological spaces. | K ₃ |
| CO4 | analyze the separation properties, convergent sequence, metric space in the general theory of topological space | K ₄ , K ₆ |
| CO5 | prove the theorems in Topological space, connectedness and compactness, countability and separation axioms, completely regular space and complete metric. | K ₃ & K ₅ |

UNIT I: TOPOLOGICAL SPACE (15 Hours)

Topological spaces – Basis for a Topology – The Order Topology – Product Topology – Closed sets and Limit Points – Continuous Functions.

UNIT II: CONNECTEDNESS(15 Hours)

Metric Topology-Connected Spaces –Connected sets in the real line –Components and path components -Local connectedness.

UNIT III: COMPACT SPACE (15 Hours)

Compact Spaces –Compact subspaces of the real line-Limit Point Compactness – Local compactness.

UNIT IV: COUNTABILITY (12 Hours)

The Countability Axioms – The Separation Axioms – Normal spaces – The Urysohn Lemma – The Urysohn Metrization Theorem .

UNIT V: THE TYCHONOFF THEOREM(15 Hours)

The Tychonoff Theorem – Completely regular spaces – The stone-Cech Compactification.

TEXT BOOK:

James R. Munkres (2005) - “Topology” ,2nd edition, Prentice Hall of India Private Limited, New Delhi.

| UNIT | CHAPTER | PAGE NUMBER |
|------|---------|---------------------|
| I | II | 75 - 111 |
| II | II,III | 119 – 133,147 - 162 |
| III | III | 163 - 185 |
| IV | IV | 189 - 218 |
| V | V | 230 - 241 |

REFERENCE BOOKS:

1. J. Dugundji, (1966) –“Topology”, Allyn and Bacon, (Reprinted in India by Prentice Hall of India Private Limited)
2. George F. Simmons,(1963) - ” Introduction to Topology and Modern Analysis”, McGraw Hill Book Company.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|---------------------|----|---|--------|
| CORE | 20MAP16 | THEORY OF NUMBERS | 72 | - | 5 |

Preamble :

To enable the students to learn and gain knowledge about Number theory.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|---|---------------------------------|
| CO1 | gain the knowledge in theory of numbers | K ₁ |
| CO2 | understand the concepts of Congruences, Quadratic reciprocity and Arithmetic functions. | K ₂ |
| CO3 | analyze and solve the problems by using Congruence formula | K ₄ & K ₅ |
| CO4 | apply Quadratic reciprocity law to solve the problems | K ₃ & K ₆ |
| CO5 | evaluate the solutions of congruences of higher degree | K ₅ |

UNIT I: INTRODUCTION TO THE CONCEPT OF NUMBERS

(15 Hours)

Introduction- Divisibility-Primes.

UNIT II: CONGRUENCES

(15 Hours)

Congruences-Solutions of congruences- Congruences of Degree 1- The functions $\phi(n)$

-Congruences of higher degree-Prime power moduli-Prime modulus.

UNIT III: CONGRUENCES**(15 Hours)**

Primitive roots and power residues-Congruences degree 2- Prime modulus-Power Residues- Number theory from an algebraic view point - Multiplicative groups-Rings and fields.

UNIT IV:QUADRATIC RECIPROCITY (15 Hours)

Quadratic residues- Quadratic reciprocity – The Jacobi Symbol.

UNIT V:ARITHMETIC FUNCTIONS**(12 Hours)**

Greatest integer function - Arithmetic functions – The Moebius Inversion formula – The multiplication of arithmetic functions .

TEXT BOOK

Ivan Nivan and HerbertsZucherman (2013) – “An Introduction to Theory of Numbers”,Fifth edition,Wiley Indian PvtLtd.,New Delhi-110002.

| UNIT | CHAPTER | SECTIONS |
|------|---------|-------------------|
| I | I | 1.1-1.3 |
| II | II | 2.1-2.3,2.6 & 2.7 |
| III | II,III | 2.8-2.11 |
| IV | III,IV | 3.1 - 3.3 |
| V | IV | 4.1-4.3 |

REFERENCE BOOKS

1. Apostol.T.M.(1995)– “Introduction to Analytic Number Theory”,FirsteditionSpringer Verlag.
2. Gareth Jones .A. & Mary Jones J.(1998) – “ Elementary Number Theory” -Springer publications.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------|-------------|-------------------------|----|---|--------|
| CORE | 20MAP17 | OPTIMIZATION TECHNIQUES | 72 | - | 4 |

Preamble :

To enable the students to learn and gain knowledge about various methods to solve the problems in Operations Research.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|---------------------------------|
| CO1 | understand the mathematical tools that are needed to solve optimization problems. | K ₂ |
| CO2 | learn how to solve the transportation problems by using various techniques and to find the shortest path for Network scheduling. | K ₃ &K ₅ |
| CO3 | evaluate the problems based on the advanced methods for large-scale transportation and assignment problems. | K ₅ , K ₆ |
| CO4 | analyze the use of basic methodology for the solution of linear programs and integer programs. | K ₄ |
| CO5 | define the basic terms under transportation problems, Network scheduling and probability. | K ₁ |

UNIT I:TRANSPORTATION PROBLEM**(15 Hours)**

Transportation problem – Introduction – Linear Programming Formulation of the Transportation Problem – Existence of Solution in T.P. – Duality in Transportation Problem – The Transportation Table – Loops in Transportation Tables – Triangular basis in a T.P. – Solution of a Transportation problem – Finding an Initial Basic Feasible Solution– MODI Method.

UNIT II:NETWORK SCHEDULING**(15 Hours)**

Network Scheduling by PERT/CPM – Introduction – Network: Basic Components – Logical Sequencing – Rules of Network Construction - Concurrent Activities - Critical Path Analysis – Distinction between PERT and CPM.

UNIT III:GAMES AND STRATEGIES**(12 Hours)**

Games and Strategies – Introduction – Two – Person Zero – Sum Games – Some Basic Terms – The Maximin – Minimax Principle – Games Without Saddle Points – Mixed Strategies.

UNIT IV:ASSIGNMENT PROBLEM**(15 Hours)**

Assignment Problem – Introduction – Mathematical formulation of the problem – Solution Methods of Assignment Problem – Special Cases in Assignment Problem.

UNIT V:PROBABILITY**(15 Hours)**

Probability – Introduction – Uncertainty and Probability – Sample Space and Probability – Algebra of Events – Conditional Probability.

TEXT BOOK:

KantiSwarup, Gupta P.K., Man Mohan (2014) – “Operations Research”, Fifteenth Thoroughly Revised Edition ,Sultan Chand and Sons, Educational Publishers, New Delhi.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|--------------------------------------|
| I | X | 10.1 – 10.09, 10.13 |
| II | XXV | 25.1 – 25.6, 25.8 (omit 25.7) |
| III | XVII | 17.1 – 17.5 |
| IV | XI | 11.1 – 11.4 |
| V | XIV | 14.1 – 14.5 |

REFERENCE BOOK:

HamdyA.Taha (2008) – “Operations Research – An Introduction”, Eighth Edition , PHI Learning Pvt. Ltd, New Delhi.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------|--------------------|---|----------|-----------|---------------|
| CORE | 20MAP18 | MATHEMATICAL SOFTWARE – II (R SOFTWARE)- PRACTICAL | - | 24 | 2 |

LIST OF PROGRAMS

All the following listed programs have to be executed and recorded

1. To use R software as a calculator.
2. To enter, manipulate and retrieval of data from gedit and Libre Office Calc to R.
3. To create data frame directly in R.
4. To display data using pie diagram, box plot, histogram and bar plot.
5. To define and call the functions in R environment.
6. To find mean, median, geometric mean, harmonic mean of numerical data.
7. To find the standard deviation, variance of the given data.
8. To find Correlation co-efficient and linear regression line for Bivariate data.
9. To find multiple linear regression models.
10. To compute probabilities in various distributions.
11. To draw the graph of probability mass and density functions.

12. To analyze the data using one and two sample 't' test and paired 't' test.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|---|-------------|------------------------|---|---|--------|
| PROFICIENCY ENHANCEMENT (SELF STUDY) | 20PEPMA01 | INDUSTRIAL MATHEMATICS | - | - | 2 |

Preamble

To enable the students to learn decision making problems based on operations research and gain the knowledge about numerical methods.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|---------------------------------|
| CO1 | understand the meaning, purpose, and tools of operations research. | K ₂ |
| CO2 | gain the knowledge about simulation, Inventory control and Numerical Methods. | K ₁ |
| CO3 | apply the concepts of Inventories to find EOQ. | K ₃ |
| CO4 | Analyze the concept of Interpolation with equal and unequal integrals and find the solution to the | K ₂ & K ₄ |

| | | |
|------------|---|-------------------------------------|
| | problems by using various methods. | |
| CO5 | evaluatethe problems based on types of inventory control. | K₅, K₆ |

Unit I:INTRODUCTION TO OPERATIONS RESEARCH

Scientific methods in O.R –Modeling in operations research – Advandages and limitations of models – Methodology of operations research – O.R and Decision Making – Applications of operations research -Opportunities and short comings of operations research.

UNIT II: SIMULATION

Introduction – Process of simulation – Simulation models – Eevent–type simulation – generation of random numbers Mmonte-carlosimulation .

UNIT-III:INVENTORY CONTROL

Types of inventories - Objectives of scientific Inventory control-Inventory costs – EOQ Problem with no shortages .

UNIT IV : INFORMATION THEORY

Introduction – Measure of information – Entropy-The expected information –Joint conditional entropies .

UNIT V: INTERPOLATION

Interpolation with equal integrals: (Central Diffrence Interpolation Formulae)

Gauss Forward formula – Gauss Backward formula - Stirling’s Formula.

Interpolation with unequal integrals:

Lagrange’s Interpolation – Inverse interpolation.

TEXT BOOK:

1. KantiSwarup, P. K. Gupta, Man Mohan (2017) –“ Operations Research” 18th Revised Edition , S. Chand & Sons Education Publications, New Delhi.
2. Dr.Venkataraman.M.K.(2013) – “Numerical Methods in Science and Engineering”, The National Publishing Company, Chennai.

| UNIT | BOOK | CHAPTER | PAGE |
|-------------|-------------|----------------|--------------------------------------|
| I | 1 | 1 | 27-35 |
| II | 1 | 22 | 639-646 |
| III | 1 | 19 | 507-524 |
| IV | 1 | 30 | 885-889, 901-903 |
| V | 2 | 7 8 | 216-225, 253-259, 262-263 |

REFERENCE BOOKS:

1. DharaniVenkata Krishnan .S – “ Operations Research Principles and Problems” Keerthi publishing house PVT Ltd.
- 2.Kandasamy. P, Thilagavathi. K and Gunavathi. K (2007) - “Numerical methods” S. Chand and Company Ltd, New Delhi – Revised Edition.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------------|------------------------|--------------------------------|-----------|----------|---------------|
| ELECTIVE - III | 20MAP19A | GRAPH THEORY | 72 | - | 4 |

Preamble:

To enable the students to learn and gain knowledge about Graphs, Euler tours, Hamiltonian cycles, Matching and Colourings of edges as well as vertices.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|----------------------|---|---|
| CO1 | understand the basic concepts of graph theory. | K₁ |
| CO2 | gain the knowledge about graph and types of graph. | K₂ |
| CO3 | apply the concepts in Euler tours and Hamiltonian cycles. | K₃ |
| CO4 | analyze the Matching and Independent sets. | K₃& K₄ |

| | | |
|------------|-------------------------|-------------------------------------|
| CO5 | Evaluate the Colouring. | K₅, K₆ |
|------------|-------------------------|-------------------------------------|

UNIT I: FUNDAMENTAL CONCEPTS OF GRAPHS AND TREES(12 Hours)

Graphs - Simple Graphs – Graph Isomorphism – The Incidence and Adjacency matrices – Subgraphs – Vertex Degrees – Paths and Connection – Cycles and trails. Trees – Cut edges and Bonds – Cut vertices – Cayley’s formula.

UNIT II:CONNECTIVITY AND PATHS (12 Hours)

Connectivity – Blocks. Euler tours and Hamilton Cycles: Euler tours – Hamilton Cycles.

UNIT III:MATCHINGS (12 Hours)

Matchings and coverings in Bipartite Graphs – Perfect Matchings. Edge colourings: Edge Chromatic number – Vizing’s theorem.

UNIT IV:INDEPENDENT SETS AND VERTEX COLOURINGS (12 Hours)

Independent sets – Chromatic Number – Brook’s Theorem – Hajo’s Conjecture.

UNITV:PLANAR GRAPHS (12 Hours)

Plane and planar Graphs – Dual Graphs – Euler’s formula – Bridges – Kuratowski’s theorem (Proof omitted) – Five Colour Theorem and Four colour Conjecture.

Text Book:

J.A.Bondy and U.S.R.Murty(1976), “Graph Theory with Applications”, American Elsevier Publishing company., Inc., New York,.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|----------------|
| I | 1 | 1.1-1.7 |
| | 2 | 2.1-2.4 |

| | | |
|------------|----------|----------------|
| II | 3 | 3.1-3.2 |
| | 4 | 4.1-4.2 |
| III | 5 | 5.1-5.3 |
| | 6 | 6.1-6.2 |
| IV | 7 | 7.1 |
| | 8 | 8.1-8.3 |
| V | 9 | 9.1-9.6 |

REFERENCE BOOKS:

1. Narsinghdeo (1987) "Graph Theory", Prentice Hall of India Private Limited, New Delhi.
2. Frank Harary, "Graph Theory", Narosa Publishing House, New Delhi.
3. R.Balakrishnan and K.Ranganathan, Springer (2008), "A Text Book of Graph Theory", New Delhi.
4. V.K. Balakrishnan, Tata Mcgrawhill (2004), " Graph Theory", Schaum's outlines, New Delhi.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------------|-------------|---------------------|----|---|--------|
| ELECTIVE - III | 20MAP19B | INTEGRAL TRANSFORMS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about Fourier Cosine and Sine Transforms and Hankel transforms.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|-----------|--|---------------------------------|
| CO1 | define the concepts based on Fourier Sine and Cosine transforms, Hankel transforms | K ₁ |
| CO2 | apply the Fourier Transforms in Laplace Equation | K ₃ |
| CO3 | gain the knowledge about the properties of Fourier and Hankel Transforms. | K ₂ |
| CO4 | analyze the problems on Fourier Transform | K ₄ |
| CO5 | evaluate the problems based on Fourier Cosine and | K ₅ , K ₆ |

| | | |
|--|---|--|
| | sine Transforms, Axisymmetric Dirichlet problems. | |
|--|---|--|

Unit I: FOURIER TRANSFORMS

(15 Hours)

Fourier sine and cosine transforms –Fourier transforms of derivatives -Fourier transforms of simple functions

Unit : II FOURIER TRANSFORMS (Con...)

(15 Hours)

Convolution integral – Parseval’s Theorem-Solution of PDE by Fourier transform –Laplace equation in half plane - Laplace equation in infinite strip –

Unit III FOURIER TRANSFORMS (Con...)

(15 Hours)

Laplace equation in semi infinite strip. The Linear diffusion equation on a semi infinite line –The two dimensional diffusion equation. Solution of the diffusion equation $\frac{\partial^2 u}{\partial x^2} = \frac{1}{k} \frac{\partial u}{\partial t}$ with the boundary condition $u_x(0,t) = f(t)$, $t \geq 0$ and the initial condition $u(x,0) = 0$ - Solution of diffusion equation on a semi infinite line.

Unit IV: HANKEL TRANSFORMS

(15 Hours)

Properties of Hankel Transforms – Hankel inversion theorem – Hankel Transform of derivative of functions - The Parseval’s relation for Henkel Transforms –Axisymmetric Dirichlet problem for a half space

Unit V HANKEL TRANSFORMS (Con...)

(12 Hours)

Axisymmetric Dirichlet problem for a thick plate. Relation between Fourier and Hankel Transforms – Problems.

TEXT BOOKS:

For Units I and II:

Sneddon.I.N.(1974) – “The Use of Integral Transforms”, Tata McGraw Hill, New Delhi.

| UNIT | CHAPTER | SECTION |
|------|---------|------------|
| I | 2 | 2.4 – 2.7 |
| II | 2 | 2.9 – 2.10 |

| | | |
|------------|----------|--|
| III | 2 | 2.16- 1(a),(b),(c), 2.16 – 2 (a), (b) |
| IV | 5 | 5.2 – 5.4, 5.6 & 5-10-1 |
| V | 5 | 5-10-2, 5.7 |

SEMESTER IV

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------|--------------------|----------------------------|-----------|----------|---------------|
| CORE | 20MAP21 | FUNCTIONAL ANALYSIS | 72 | - | 5 |

Preamble

To enable the students to learn and gain knowledge about Banach spaces and Hilbert spaces.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|---|--|
| CO1 | understand the basic concept of Banach spaces, Continuous linear functional, Bounded linear operator, Hilbert spaces and operators. | K₁ |
| CO2 | Gain the knowledge about Banach space, Hilbert | K₁ & K₂ |

| | | |
|------------|--|--|
| | space and the conjugate of an operator. | |
| CO3 | apply the knowledge of functional analysis to solve mathematical problems. | K₃&K₅ |
| CO4 | analyze some basic properties by using metric spaces, normed linear space, parallelogram law, orthogonal complements, the adjoint operators, projection theorem. | K₄ |
| CO5 | establish the weak and weak* topology, complete orthogonal set, complete orthonormal set adjoint operators and projection operators. | K₅, K₆ |

UNIT I: BANACH SPACES

(15 Hours)

Introduction- Basic inequalities –Metric Space and its properties –Vector space – Normed linear spaces, Definitions and properties-Examples of Banach spaces-Quotient spaces-Direct sum of subspace-Continuous linear transformations.

UNIT II: CONTINUOUS LINEAR FUNCTIONALS

(15 Hours)

Introduction- continuous linear functional-Representation theorems for functional-The Hahn Banach Theorem-Some consequences of the Hahn Banach Theorems.

UNIT III: BOUNDED LINEAR OPERATORS

(15 Hours)

Introduction-The open mapping theorem-The closed graph theorem-The Banach-Steinhaus theorem-The Weak and Weak* Convergence-The conjugate of an operator.

UNIT IV: HILBERT SPACE (15 Hours)

Introduction- Definitions and Examples-Hilbert space and its basic properties-Applications of the parallelogram law-Orthogonal Complements-The Orthogonal Decomposition Theorem-Orthonormal sets-Complete orthogonal sets.

UNIT V: OPERATORS ON HILBERT SPACES (12 Hours)

Introduction-The adjoint Operator-Self adjoint operator-Normal operator-Unitary operator-Projection operators.

TEXT BOOK:

D.Somasundaram(2013) - “A First Course in Functional Analysis ”,Third Re-Print , Narosa Publishing House,New Delhi.

| Unit | Chapter | Sections |
|-------------|----------------|--------------------------|
| I | I | 1.1 – 1.9 |
| II | II | 2.1-2.5 |
| III | III | 3.1 –3.2, 3.4-3.7 |
| IV | IV | 4.1 -- 4.9 |
| V | V | 5.1 – 5.6 |

REFERENCE BOOKS:

1 .C. Goffman and G. Pedrick(1987) - “A First Course in Functional Analysis”, Prentice Hall of India, New Delhi.

2.G.F. Simmons(1963) - “Introduction to Topology and Modern Analysis”, McGraw –Hill Book Company, London.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-----------------|--------------------|-----------------------------|-----------|----------|---------------|
| CORE | 20MAP22 | MATHEMATICAL METHODS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about Integral Equations and Calculus of Variations.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|--|--|
| CO1 | Define the concepts based on Various types of integral equations and Calculus of Variations. | K₁ |
| CO2 | apply the integral equations in ordinary differential | K₄ & K₃ |

| | | |
|------------|---|--|
| | equations. | |
| CO3 | Understand the various types of integral equations | K₂ |
| CO4 | Learn and analyze the concepts of Fredholm Integral Equation and Volterra Integral equation, Calculus of Variation. | K₂ & K₄ |
| CO5 | evaluate the problems based on Fredholm Integral Equation and Volterra Integral equations. | K₅, K₆ |

Unit I: INTEGRAL EQUATIONS

Types of Integral equations –Integral Fredholm Alternative–Equation with separable Kernel.

Unit II: METHOD OF SUCCESSIVE APPROXIMATIONS

Method of successive Approximations – Iterative Scheme - Volterra integral equations – examples.

Unit III: SINGULAR & ABEL INTEGRAL EQUATIONS

Application of Integral equation to ordinary differential equation –Initial value problems – Boundary value problems –Singular integral equations –Abel Integral equation.

Unit IV: CALCULUS OF VARIATIONS

Variation and its properties – Fundamental lemma of calculus of variations - Euler’s equation – Functionals of the integral forms -Functional dependent on higher order derivatives – Euler poisson equations.

Unit V: CALCULUS OF VARIATIONS (Con...)

Functionals dependent on the functions of several independent variables – Ostrogradsky equation - Variational problems in parametric form –Applications.

TEXT BOOKS:

For Units III and IV:

Kanwal.R.P. (1971) – “Linear Integral Equations Theory and Technique” , Academic press, New York.

For Unit V:

Elsgolts.L. (1970) – “Differential Equations and Calculus of Variations”, Mir publishers, Moscow.

| UNIT | CHAPTER | SECTION |
|------------|-------------|------------------|
| I | I | 1.1 – 1.6 |
| | II | 2.3 – 2.5 |
| II | III | 3.1 – 3.4 |
| III | V | 5.1 – 5.2 |
| | VIII | 8.1 – 8.2 |
| IV | VI | 6.1 – 6.4 |
| V | VI | 6.5 – 6.7 |

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|-------------|----------------|-----------------------|-----------|----------|----------|
| CORE | 20MAP23 | FLUID DYNAMICS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about the concept of energy equation and boundary layer in compressible and incompressible flow.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------|---|----------------------|
| CO1 | define the concepts based on compressible and incompressible flow, stream lines ,path lines, velocity, density and pressure, source and sink, vortex. | K₁ |

| | | |
|------------|--|--|
| CO2 | analyze and apply the concepts of fluid dynamics in momentum theorem, Blasius theorem and Navier Stokes equations. | K₄ & K₃ |
| CO3 | gain the knowledge about vorticity and circulation in various fluid, conservative forces and boundary layer equations. | K₂ |
| CO4 | learn and analyze the concepts based on displacement thickness, momentum thickness and kinetic energy thickness. | K₂ & K₄ |
| CO5 | evaluate the problems based on stream lines, path lines in two – dimensional motion. | K₅, K₆ |

Unit I: STREAM LINES AND PATH LINES

(15 Hours)

Introductory Motions – Velocity – Stream Lines and Path Lines – Stream Tubes and Filaments – Fluid Body – Density – Pressure. Differentiation following the Fluid – Equation of continuity – Boundary conditions – Kinematical and physical – Rate of change of linear momentum – Equation of motion of an inviscid fluid.

Unit II: ENERGY EQUATION FOR INVISCID FLUID:

(15 Hours)

Euler’s momentum Theorem – Conservative forces – Bernoulli’s theorem in steady motion – Energy equation for inviscid fluid – circulation – Kelvin’s theorem – Vortex motion – Helmholtz equation.

Unit III: TWO DIMENSIONAL MOTION:

(15 Hours)

Two Dimensional Motion – Two Dimensional Functions – Complex Potential – Basic singularities – Source – Sink – Vortex – Doublet – Circle theorem. Flow past a circular cylinder with circulation – Blasius Theorem – Lift force. (Magnus effect)

Unit IV: NAVIER-STOKES EQUATIONS:

(15 Hours)

Viscous flows – Navier-Stokes equations – Vorticity and circulation in a viscous fluid – Steady flow through an arbitrary cylinder under pressure – Steady Couette flow between cylinders in relative motion .

Unit V: BOUNDARY LAYER EQUATIONS**(12 Hours)**

Laminar Boundary Layer in incompressible flow: Boundary Layer concept – Boundary Layer equations – Displacement thickness, Momentum thickness – Kinetic energy thickness – Integral equation of boundary layer – Flow parallel to semi infinite flat plate – Blasius equation and its solution in series.

TEXT BOOKS:**For Units I and II:**

Milne Thomson. L.M. (1968) – “Theoretical Hydro Dynamics”, 5th Edition, McMillan Company.

For Units III, IV and V:

Curle. Nand Davies. H.J (1968) – “Modern Fluid Dynamics” – (Volume I) D Van Nostrand Company Limited, London.

| UNIT | CHAPTER | SECTION |
|------|---------|--|
| I | I | 1.0 – 1.3., 3.10-3.41 (omit 3.32) |
| II | III | 3.42 – 3.53 (omit 3.44) |
| III | III | 3.1 – 3.7.5 (omit 3.3.4, 3.4, 3.5.3, 3.6) |
| IV | V | 5.1 – 5.3.2 |
| V | VI | 6.1 – 6.3.1 (omit 6.2.2., 6.2.5) |

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------------------|--------------------|-----------------------------------|-----------|----------|---------------|
| ELECTIVE - IV | 20MAP25A | FUZZY LOGIC AND FUZZY SETS | 72 | - | 4 |

Preamble

To enable the students to learn and gain knowledge about fuzzy sets, fuzzy relations, fuzzy measures, uncertainty and information and also their applications.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|---|---|
| CO1 | gain the knowledge about fundamentals of fuzzy set theory with fuzzy logic. | K₁& K₂ |
| CO2 | apply the concepts of fuzzy sets in | K₃ |

| | | |
|------------|--|-------------------------------------|
| | fuzzy relations. | |
| CO3 | analyze the fuzzy measures. | K₃ |
| CO4 | evaluate the fuzzy logic in various types of uncertainty | K₄ |
| CO5 | evaluate their relation to information and complexity. | K₅, K₆ |

UNIT – I: CRISP SETS AND FUZZY SETS (12 Hours)

The Notion of Fuzzy sets – basic concepts of Fuzzy sets – Fuzzy complement – Fuzzy union – Fuzzy intersection.

UNIT – II : FUZZY RELATIONS (15 Hours)

Crisp and Fuzzy relations – Binary relations – Binary relations on a single set – Equivalence and similarity relations.

UNIT – III :FUZZY MEASURES (15Hours)

Belief and plausibility Measures – Probability measures – Possibility and Necessity measures.

UNIT –IV : UNCERTAINTY AND INFORMATION (15 Hours)

Types of Uncertainty – Measures of Fuzziness – Classical measures of Uncertainty – Hartley information – Shannon entropy - Measures of Dissonance – Measures of confusion – Measures of Non-Specificity.

UNIT – V :UNCERTAINTY AND INFORMATION (15 Hours)

General discussion – Natural, life and social sciences – Management and decision making – Computer Science.

TEXT BOOK:

George J. Klir and Tina A. Folger, (1995) - "Fuzzy Sets, Uncertainty and Information",
Prentice-Hall of India Private Limited.

| UNIT | CHAPTER | SECTION |
|-------------|----------------|------------------|
| I | 1 | 1.3-1.4 |
| | 2 | 2.2-2.4 |
| II | 3 | 3.1-3.4 |
| III | 4 | 4.2-4.4 |
| IV | 5 | 5.1-5.6 |
| V | 6 | 6.1 – 6.6 |

REFERENCE BOOK:

George J. Klir and Boyuan, "Fuzzy Sets and Fuzzy Logic – Theory and Applications", Prentice-Hall
of India Private Limited.

| CATEGORY | COURSE CODE | TITLE OF THE COURSE | C | P | CREDIT |
|----------------------|--------------------|------------------------------|-----------|----------|---------------|
| ELECTIVE - IV | 20MAP25B | ACTUARIAL MATHEMATICS | 72 | - | 4 |

Preamble

To teach the students about Annuities, Premium calculation, Commutation functions, Population functions and risk models.

Course Outcomes

On the successful completion of the course, students will be able to

| CO NUMBER | CO STATEMENT | KNOWLEDGE LEVEL |
|------------------|---|--|
| CO1 | gain the knowledge about fundamentals of probability and Annuities. | K₁ & K₂ |

| | | |
|------------|---|-------------------------------------|
| CO2 | apply Statistical tools in Life insurance related problems. | K₃ |
| CO3 | analyze the Premium Calculation. | K₃ |
| CO4 | evaluateSome Special Integrals in probability. | K₄ |
| CO5 | evaluate the use of demographic concepts and population theories to understand contemporary socio-economic issues and current affairs | K₅, K₆ |

UNIT I BASICS OF PROBABILITY AND INTEREST: (12 Hours)

Probability - Theory of Interest: Variable Interest Rates -Continuous-time Payment Streams – Problems. Interest& Force of Mortality: More on Theory of Interest - Annuities & Actuarial Notation -Loan Amortization & Mortgage Refinancing - Illustration on Mortgage Refinancing – Computational illustration in Splus - Coupon & Zero-coupon Bonds Force of Mortality & Analytical Models: Comparison of Forces of Mortality – Problems .

UNIT II PROBABILITY & LIFE TABLES: (15 Hours)

Interpreting Force of Mortality - Interpolation Between Integer Ages - Binomial Variables & Law of Large Numbers: Exact Probabilities, Bounds & Approximations - Simulation of Life Table Data: Expectation for Discrete Random Variables -Rules for Manipulating Expectations - Some Special Integrals – Problems .

Expected Present Values of Payments: Expected Payment Values: Types of Insurance & Life Annuity Contracts - Formal Relations among Net Single Premiums - Formulas for Net Single Premiums - Expected Present Values for $m = 1$ - Continuous Contracts & Residual Life: Numerical Calculations of Life Expectancies – Problems.

UNIT III COMMUTATION & RESERVES: (15 Hours)

University of Maryland, College Park, Edition 2001

Reference Books:

1. Jerry Alan Veeh, Lecture Notes on Actuarial Mathematics (E-notes), 2006.
2. Bowers, N., Gerber, H., Hickman, J., Jones, D. and Nesbitt, C. Actuarial Mathematics, Society of Actuaries, Itasca, Ill. 1986.
3. Feller, W. An Introduction to Probability Theory and its Applications, vol.I, 2nd ed. Wiley, New York, 1957.
4. Gerber, H. Life Insurance Mathematics, 3rd ed. Springer-Verlag, New York, 1997.
5. Hogg, R. V. and Tanis, E. Probability and Statistical Inference, 5th ed. Prentice-Hall Simon & Schuster, New York, 1997.



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